

Course # 0510.6802

Spectral Methods for Excitation and Radiation of Fields and Waves

Course plan

1. Derivation of the basic equations governing the radiation from sources in a layered medium (2 meetings)
 - a. Scalarization of the field equations
 - b. One-dimensional transmission-line equations
 - c. The 2D spectral integral and its reduction with the Fourier-Bessel transform
2. A source in the presence of a dielectric half-space (2 meetings)
 - a. Spectral representations in 2D, 3D, and the passage to 2.5D via the FBR
 - b. Analytic properties in the complex spectral plane and angular spectrum plane
3. Asymptotic evaluation of integrals and spectral plane implementation (2 meetings)
 - a. Identification of analytic properties
 - i. Saddle point contribution
 - ii. Contributions from singular points: poles and branch cuts
 - b. Interpretation of the various contributions as different wave phenomena.
 - i. Wave phenomena – transmitted and reflected waves, the Head wave.
 - ii. Canonical representations
 - c. Home assignment: Transmitted field in 2D, and 3D problem via the FBR
4. Strum-Liouville theory (2 meetings)
 - a. The set of eigenfunctions and eigenvalues. Discrete spectrum. Continuous spectrum
 - b. Characteristic Green's function and the construction of the complete spectrum
 - c. Completeness relations
 - d. Green's function alternative representations
5. Parallel planes waveguide (2 meetings)

- a. Alternative representations – modes and rays
 - b. Hybrid Ray-Mode representations
 - c. The dielectric waveguide and generalization to multilayer media
 - d. Home assignment
6. Continuous layered medium (2 meetings)
- a. The mapping to canonical equations (WKB and its generalization) and rays interpretation
 - b. Bremmer series
7. Electrically small scatterers in layered media (?) (1 meeting)

Bibliography

- [1] L.B. Felsen and N. Marcuvitz, *Radiation and Scattering of Waves*, Prentice Hall N.J. 1973 (reissued by IEEE Press series on Electromagnetic Wave Theory).
- [2] Weng C. Chew, *Waves and Fields in Inhomogeneous Media*, Van Nostrand Reinhold, N.Y. 1990 (reissued by IEEE Press series on Electromagnetic Wave Theory).
- [3] A. Ishimaru, *Electromagnetic Wave Propagation, Radiation, and Scattering*, Prentice Hall N.J. 1991.
- [4] Course booklet – available for download in the course site in moodle.